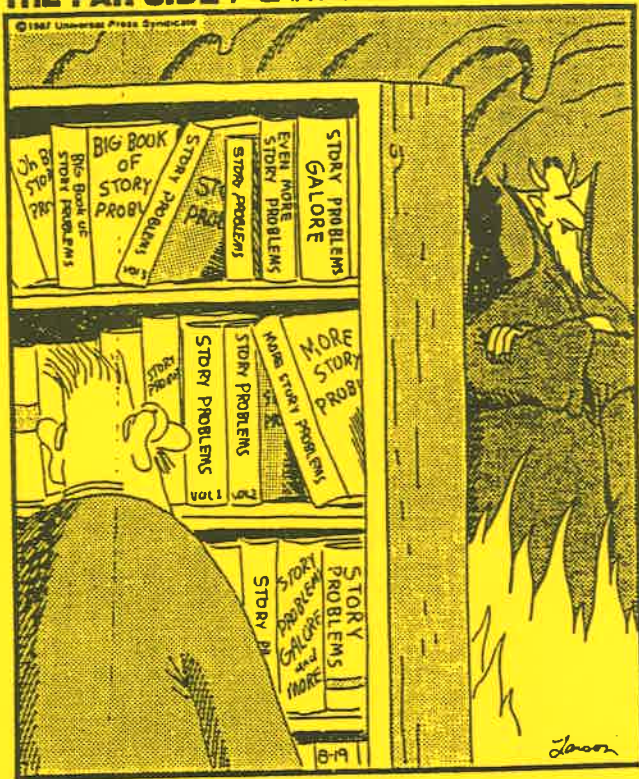


**1989**  
**Washington**  
**Community**  
**College**  
**Mathematics**  
**Retreat**

**Campbell's Resort**  
**Lake Chelan**

**April 20 - 22**

# THE FAR SIDE / GARY LARSON



HELL'S LIBRARY

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- **Mathematical Trivia Test**
- **Schedule of Events**
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- **Acknowledgements**

## PARTICIPANTS

### BELLEVUE COMM. COLL.

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Larry & Kathy Curnutt  
Dale Hoffman  
Rose Pugh  
Pete & Laurence Ratener  
Jim & Judie Relf  
Dave Stacy

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Margaret & Stephen Lane

### BOEING COMPANY

Dave & Mary Jo Hiestand

### CENTRAL WASHINGTON U.

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### CLARK COLLEGE

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Louise Hoover  
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PENNINSULA COLLEGE

Kent & Rosemary Brauningner

PEPPERDINE UNIVERSITY

Louis Leithold

PIERCE COMM. COLL.

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Deb Falcioni  
Sally Glover-Richard  
Michael Lamka  
John Van Druff

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Dick Clark  
Patrick & Shirley Clock

SEATTLE CENTRAL COMM. COLL.

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SEATTLE UNIVERSITY

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Mark Parker  
Steve Perry  
Larry & Holly Runyan

SKAGIT VALLEY COMM. COLL.

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UNIV. OF WASHINGTON

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WASHINGTON STATE UNIV.

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WESTERN WASHINGTON UNIV.

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Ibrahim Ayyoub  
James Hutchison  
Aziz & Kathryn Jubran  
Roger & Ellena Knobel  
Douglas Lewis  
Ben Mayo  
Larry Ozanich

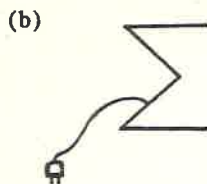
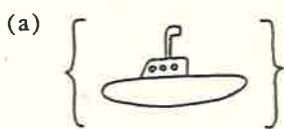
# TRIVIA

# MATHEMATICA

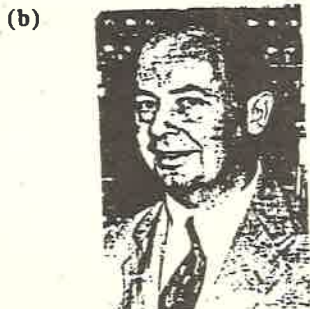
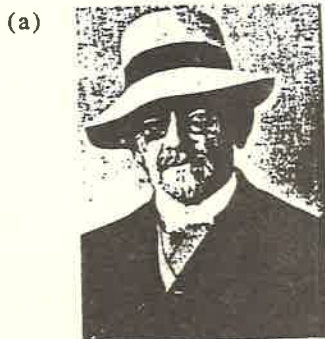
Play alone or play as a group.

Win a book for your personal collection or school library.  
Prizes will be awarded at lunch on Saturday.

1. Besides his Rule, what else is L'Hopital famous for?
2. Where was Georg Cantor when he died?
3. Who is "the father of fractals?"
4.  $V - E + F = ?$
5. What is Underwood Dudley's Erdős number?
6. What calculus book was used by Jaime Escalante's class in the motion picture "Stand and Deliver?"
7. Who wrote "*Beauty is the first test; there is no permanent place in the world for ugly mathematics.*" ?
8. Name two Fields Medalists.
9. Translate. (Each Rebus represents the name of a mathematical object)



10. Identify.



# ANSWER SHEET

Tear out this page.  
Turn in your answers at breakfast on Saturday.

Name \_\_\_\_\_ School \_\_\_\_\_

1. \_\_\_\_\_

2. \_\_\_\_\_

3. \_\_\_\_\_

4. \_\_\_\_\_ 5. \_\_\_\_\_

6. \_\_\_\_\_

7. \_\_\_\_\_

8. \_\_\_\_\_

9. (a) \_\_\_\_\_ (b) \_\_\_\_\_

10. (a) \_\_\_\_\_ (b) \_\_\_\_\_

**TIE-BREAKER:** (scored subjectively in case of tie)

If mathematicians were in charge of the movie industry, they might produce films like "Raiders of the Lost Arctan." If mathematicians controlled the paperback novel business, what title might we look forward to on the best seller lists?

Notes



## SCHEDULE OF EVENTS

### Thursday, April 20

- 5:00 - 7:00 pm Registration (dinner on your own)
- 7:00 - 8:30 pm Talks (Ballroom 3)
- 9:00 - ?:00 pm Hospitality (River Room)  
Movie: "Stand and Deliver"  
(Auxiliary Conference Center)  
Videotapes: For All Practical Purposes  
(Edmunds Room)

### Friday, April 21

- 8:00 - 9:15 am Continental Breakfast (Ballroom 1)
- 9:30 - 11:00 am Talks (Ballrooms 2 and 3)
- 11:30 - 12:45 am Lunch (Auxiliary Conference Center)
- 1:00 - 4:30 pm Afternoon Talks (Ballrooms 1, 2, and 3)
- 6:00 - 7:00 pm No host cocktails (Ballroom foyer)
- 7:00 - 9:00 pm BANQUET (Ballroom) +  
"Mathematical Cranks" by Underwood Dudley
- 9:00 - ?:00 pm "Stand and Deliver" (Ballroom 3)  
For All Practical Purposes (Edmunds Room)  
applied probability

### Saturday, April 22

- 7:30 - 8:15 am Breakfast Buffet (Dining Room)
- 8:30 - 11:30 am Talks (Ballrooms 1, 2, and 3)
- 12:00 - 1:15 pm Lunch (Auxiliary Conference Center)
- 1:30 - ?:00 pm WAMATYC meeting

Thursday Evening

Ballroom 3

7:00 - 7:40 pm	"Numeration as a Precursor to Writing" David Stacy, BCC
7:50 - 8:30 pm	"Problem Solving: A Useful Tool in Everyday Life" Gail Nord, GU
9:00 pm	"Stand and Deliver" movie and <u>For All Practical Purposes</u> videos + applied probability practice

Friday Morning

Ballroom 2

Ballroom 3

9:30 - 10:00 am	"Strategies for Success with Developmental Classes" David Hemme, SCCC	"Another Look at the Countability of the Rationals" Andre Yandl, SU
10:30 - 11:00 am	"Effective Student Placement Testing" Stephen Hinthorne, CWU	"Oddities About Triangular Numbers" James Jordan, WSU

Friday Afternoon

Ballroom 1

Ballroom 2

Ballroom 3

1:00 <del>1:45</del> pm	"The Mathematical Modeling of a Slash Burn" Phil Heft, GRCC	"Limit Cycles in First Order D.E.s" Susan Gardsbane, WWU	"Working a Straight Line Through Rough Terrain" Dick Clark, PCC
2:00 - 2:45 pm	"Dollar-Cost Averaging: Does It Really Work?" Elmar Zengalis, HCC	"For What $n$ is $a^n \equiv a \pmod{n}, \forall a$ ?" Martin Haines, OC	"Calculus for a New Century: A Report" Dale Hoffman, BCC
3:00 - 3:45 pm	"The Largest Pyramidal Box" Larry Larson, GRCC	"Highly Composite Numbers" John Reay, WWU	"An Exceptional Class For Exceptional Students" Dorothy Crepin, CC

East-West Room (upstairs)

4:00 - 4:30 pm	"What's Happening At The U of W?" Casper Curjel, UW
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Saturday Morning

Ballroom 1

Ballroom 2

Ballroom 3

8:30 - 9:15 am	"A Computer Algorithm for Solving Alphametics" Mark Parker, ShCC	"Mathematics Competitions" Jim Relf, BCC	"Applications of Linear Algebra" Rich Levin, WWU
9:30 - 10:15 am	"Mathematical Computer Graphics" Yves Nievergelt, EWU	"The Normal to the Curve Represented by the Equation if $y = x + \sin(xy)$ then $dy/dx$ ; or What Happened saturday, March 12, 1988." Louis Leithold, PU	"Tic-Tac-Toe in Higher Dimensions" Norm Lindquist, WWU
10:45 - 11:30 am		"Multivariable Calculus — Some Points of View" Casper Curjel, UW	"Monsters, Dragons, and Chaos" Dave Hiestand, Boeing

**ABSTRACTS**  
(alphabetical by presenter)

**CLARK, Dick.** Portland Community College  
*"Working a Straight Line Through Rough Terrain"*  
1:00 - 1:45                      Friday                      Ballroom 3  
Too often we teach integrated topics as isolated entities. The real number line is an ideal thread to weave through freshman and sophomore mathematics. Exploiting the critical point concept in this context can reduce fear and frustration.

**CREPIN, Dorothy.** Clark College  
*"An Exceptional Class for Exceptional Students"*  
3:00 - 3:45                      Friday                      Ballroom 3  
Novel experiences with a class of anxious math avoiders. Material from pre-algebra through intermediate algebra was covered in three quarters. A multi-faceted approach proved effective -- video tapes, group activities, personal journals, frequent class evaluations, exercises to alleviate anxiety, innovative testing procedures.

**CURJEL, Casper.** University of Washington  
*"What's Happening at the U of W?"*  
4:00 - 4:30                      Friday                      East-West Room  
An informal discussion of the U of W's changes in calculus, linear algebra, and differential equations curricula. What they are, and how they're working.

**CURJEL, Casper.** University of Washington  
*"Multivariable Calculus -- Some Points of View"*  
10:45 - 11:30                      Saturday                      Ballroom 2  
In multivariable calculus even solid students have difficulties working problems that are moderately different from those done in class. It cannot all be the students' fault. This is a report on attempts to restructure some of the material and its presentation.

**DUDLEY, Underwood.** DePauw University  
*"Mathematical Cranks"*  
8:00 - 9:00 pm                      Friday                      Ballroom  
When mathematical cranks are mentioned, most people think only of angle trisectors, circle squarers, and perhaps provers of Fermat's Last Theorem, and dismiss them with, "Oh, those nuts" or something similar. This is too narrow a view. Mathematical cranks are of all sorts and they attack an amazing variety of problems (and non-problems). This talk aims to give a survey of this rich and little-known field.

**GARDSBANE, Susan.** Western Washington University  
*"Limit Cycles in First Order Differential Equations"*  
1:00 - 1:45 Friday Ballroom 2  
Hilbert's 16th problem asks for the number and position of limit cycles of first order differential equations. A summary of recent research on the problem, examples, and some surprising results for differential equations of degree two.

**HAINES, Martin.** Olympic College  
*"For What  $n$  is  $a^n = a \pmod n$ , for all  $a$ ?"*  
2:00 - 2:45 Friday Ballroom 2  
Prime numbers have this property. We'll see which composite numbers do. It will be truly elementary, with an almost incidental bit of group theory. The significance is dubious! Teaser:  $n = 1729 = 7 \times 13 \times 19$  is such a value.

**HEFT, Phil.** Green River Community College  
*"The Mathematical Modeling of a Slash Burn"*  
1:00 - 1:45 Friday Ballroom 1  
The forest service sometimes hangs instruments over a slash burn to get data on temperature, vertical velocities of the air, and the combustive products produced. The intensity of the fire can then be modeled as a function of time.

**HEMME, David.** Seattle Central Community College  
*"Strategies for Success with Developmental Classes"*  
9:30 - 10:00 Friday Ballroom 2  
Overcoming anxiety. Ideas that work with remedial, technical, and lab courses.

**HIESTAND, David.** Boeing Company  
*"Monsters, Dragons and Chaos"*  
10:45 - 11:30 Saturday Ballroom 3  
A non-technical discussion of fractals and their use in landscapes, image compression, and chaos theory. This computer slideshow-like presentation includes dramatic pictures of the Mandelbrot Set, Julia sets, and chaotic dynamic systems.

**HINTHORNE, Stephen.** Central Washington University  
*"Effective Student Placement Testing"*  
10:30 - 11:00 Friday Ballroom 2  
How do we effectively ensure correct placement in the mathematics curriculum for incoming, first-time and transfer students? How do the present tests measure up? Do students who pass succeed?

**HOFFMAN, Dale.** Bellevue Community College

*"Calculus for a New Century: A Report":*

2:00 - 2:45                      Friday                      Ballroom 3

What's all the fuss? Who's trying what? What are the early results? Where is it going? This is a report by an attendee at the Calculus for a New Century Conference (November, 1987) and the MAA-AMS Winter Meeting (January, 1989).

**JORDAN, James.** Washington State University

*"Oddities About Triangular Numbers"*

10:30 - 11:00                      Friday                      Ballroom 3

When represented in odd bases, triangular numbers (1,3,6,10,15,....) have many interesting properties. For example, in base twenty-five, the numbers represented by 3, 33, 333, 3333, ..... are all triangular numbers.

**LARSON, Larry.** Green River Community College

*"The Largest Pyramidal Box"*

3:00 - 3:45                      Friday                      Ballroom 1

Maximizing the volume of the frustrum of the pyramid formed by removing wedge-shaped pieces from the corners of a square and folding up the sides.

**LEITHOLD, Louis.** Harper & Row ,Inc./Pepperdine University

*"The Normal to the Curve Represented by the Equation if  $y = x + \sin(xy)$  then  $dy/dx$ ; or What Happened Saturday, March 12, 1988."*

9:30 - 10:15                      Saturday                      Ballroom 2

This is the actual title! I did not make a typing error. The title will make sense when you hear the presentation.

**LEVIN, Richard.** Western Washington University

*"Applications of Linear Algebra"*

8:30 - 9:15                      Saturday                      Ballroom 3

Some interesting applications of linear algebra which can be used to motivate the study of this subject. Cubic splines, partial differential equations, and systems of non-linear equations.

**LINDQUIST, Norm.** Western Washington University

*"Tic-Tac-Toe in Higher Dimensions"*

9:30 - 10:15                      Saturday                      Ballroom 3

Using the game of tic-tac-toe as a model for higher dimensions. The participants will learn how to play 4-dimensional tic-tac-toe.

**NIEVERGELT, Yves.** Eastern Washington University  
*"Mathematical Computer Graphics (not necessarily on the HP-28S)"*

9:30 - 10:15                      Saturday                      Ballroom 1

This is a preview of a minicourse to be given in June at MIT. (1) 3D-graphics in calculus; (2) fractals from precalculus through analysis; (3) cubic splines in linear algebra. This show demonstrates theory, exercises for students, and supercalculator programs.

**NORD, Gail.** Gonzaga University  
*"Problem Solving: A Useful Tool in Everyday Life"*

7:50 - 8:30                      Thursday                      Ballroom 3

We will examine the Tower of Hanoi, an integer path problem, and a checkerboard problem. We will examine the tools of subgoaling, proof by contradiction, and working backwards.

**PARKER, Mark.** Shoreline Community College  
*"A Computer Algorithm for Solving Alphametics"*

8:30 - 9:15                      Saturday                      Ballroom 1

An algorithm, implemented in Apple Pascal, for solving the word addition problems that appear often in the daily newspaper. How the basic algorithm can be helped along in the most difficult problem types.

**REAY, John.** Western Washington University  
*"Highly Composite Numbers"*

3:00 - 3:45                      Friday                      Ballroom 2

Intuitively, an integer is highly composite if it has 'lots' of divisors. To give small integers a fair chance, we say that  $n$  is highly composite if it has more divisors than any smaller positive integer. How many HCN's are there? Is there an efficient algorithm for identifying HCN's? Come help answer these and other interesting questions about HCN's.

**RELF, Jim.** Bellevue Community College  
*"Mathematics Competitions"*

8:30 - 9:15                      Saturday                      Ballroom 2

What is the NATIONAL STUDENT MATHEMATICS LEAGUE, and how do you get involved? Participating in AMATYC sponsored math competitions has inspired a surprising amount of student enthusiasm and some entertaining professional development for the faculty. Examples of typical test questions will be presented.

**STACY, David.** Bellevue Community College

*"Numeration as a Precursor to Writing"*

7:00 - 7:40

Thursday

Ballroom 3

Recent investigation has serendipitously revealed that early counting with "tokens" evolved into the pictographic writing of the Sumerians.

**YANDL, Andre.** Seattle University

*"Another Look at the Countability of the Rationals"*

9:30 - 10:00

Friday

Ballroom 3

We derive a closed formula which defines a 1-1 function from  $\mathbb{I} \times \mathbb{I}$  onto  $\mathbb{I}$ .

**ZEMGALIS, Elmar.** Highline Community College

*"Dollar-cost Averaging: Does It Really Work?"*

2:00 - 2:45

Friday

Ballroom 1

Investment counsellors advocate dollar-cost averaging as an investment strategy. A mathematical analysis of their claims leads to some rather difficult, novel, and intriguing conjectures involving inequalities and multiple integrals.

**A VERY BRIEF HISTORY OF THE  
WASHINGTON COMMUNITY COLLEGE  
MATHEMATICS RETREAT**

<u>YEAR</u>	<u>HOST</u>	<u>LOCATION</u>
1989	Bellevue Community College	Chelan
1988	Olympic Community College	Port Ludlow
1987	Lower Columbia College	Alderbrook
1986	North Seattle Community College	Alderbrook
1985	Shoreline Community College	Sun Mountain
1984	Green River Community College	Alderbrook
1983	Olympic Community College	Port Ludlow
1982	Highline Community College	Chelan
1981	Spokane Falls Community College	Sun Mountain
1980	Spokane Falls Community College	Sun Mountain
1979	Olympic Community College	Port Ludlow
1978	Edmonds Community College	Providence Heights
1977	Shoreline Community College	Providence Heights
1976	Bellevue Community College	Snoqualmie Pass
1975	Highline Community College	Providence Heights
1974	Shoreline Community College	Lake Wilderness
1973	?	?
1972	?	?
1971	?	?
1970	Spokane Falls Community College	Snoqualmie Pass
1969	Green River Community College	?
1968	?	?
1967	?	?

1966      The first Washington Community College Mathematics retreat was organized by Phil Heft, Larry Larson, Jim Relf, and John VanDruff. 33 participants met at the "lodge" at Ashford with sleeping bags. The cost was \$16.68 per person.

??? Do you see any errors in this chronology? Can you fill in any of the blanks? Hand or mail your corrections and additions to Larry Curnutt, Bellevue Community College.



Notes

Members of the mathematics faculty at Bellevue Community College have enjoyed organizing the 1989 Washington Community College Mathematics Retreat for you. Even more, we enjoy passing the responsibility on to \_\_\_\_\_?\_\_\_\_\_ for 1990.

We would like to extend special thanks to our guests

**UNDERWOOD DUDLEY and  
LOUIS LEITHOLD**

for their contributions to this conference; to

**HARPER & ROW PUBLISHERS**

for underwriting Professor Leithold's participation; to

**MCGRAW-HILL BOOK COMPANY and  
JOHN WILEY & SONS**

for donating some of the prizes for the trivia game; and to

**ALL OF YOU**

for your good company and continued support of this little gathering  
(going on twenty-five years, now!).

See you next spring at \_\_\_\_\_?\_\_\_\_\_.

The first part of the document discusses the importance of maintaining accurate records of all transactions. It emphasizes that every entry, no matter how small, should be recorded to ensure the integrity of the financial data. This includes not only sales and purchases but also expenses and income. The text suggests that a systematic approach to record-keeping is essential for identifying trends and making informed decisions.

In the second section, the author addresses the challenges of managing cash flow. It is noted that many businesses struggle with timing their payments and receipts. The text provides several strategies to improve cash flow, such as offering discounts for early payment and negotiating longer terms with suppliers. It also stresses the importance of regularly reviewing the cash flow statement to stay on top of the company's financial health.

The third part of the document focuses on budgeting and cost control. It explains how a well-defined budget can help a business allocate resources effectively and avoid unnecessary expenditures. The author provides tips on how to track actual costs against budgeted amounts and identify areas where savings can be made. It also discusses the importance of reviewing the budget regularly to adjust to changing market conditions.

Finally, the document concludes with a section on financial reporting. It outlines the key components of a financial statement, including the balance sheet, income statement, and cash flow statement. The text provides guidance on how to prepare these statements accurately and how to interpret the results. It also mentions the importance of seeking professional advice when needed to ensure compliance with accounting standards.